

Unit-3

searching and sorting

1) Linear or sequential search -

Concept → Enter array size $N=5$

Enter array element

10 8 12 6 14

Enter item to be searched

$e=6$ or $e=16$

$i=0$

↓

↓

10

8

12

6

14

* $if (e == a[i])$

found

otherwise

$i++;$

} repeat these steps while $(i \leq N)$

$if (i == N)$

not found

case 1 → $e=6$

Algorithm

1. $i=0$

$e == a[i]$

$6 == 10$ False $i=1$

2. $i=1$

$6 == 8$ False set $i=2$

3. $i=2$

$6 == 12$ False set $i=3$

4. $i=3$

$6 == 6$ True found

case 2 →

$e=13$

1. $i=0$

$13 == 10$ False $i=1$

2. $i=1$

$13 == 8$ False $i=2$

3. $i=2$

$13 == 12$ False $i=3$

4. $i=3$

$13 == 6$ False $i=4$

5. $i=4$

$13 == 14$ False $i=5$

$i=5 \Rightarrow$ False Exit from loop $i=5 \Rightarrow$ True Not found

Algorithm → Linear Search ($A[\text{maxsize}], N$)

1. Read $N, f=0$
2. Read Array elements
3. Read element to be searched (item)
4. Set $i = lb$
5. While ($i \leq ub$)
 6. If ($A[i] = \text{item}$)
 write "found"
 set $f=1$
 [End of if]
 7. ~~set~~ set $i=i+1$
 [End of loop]
8. If ($f=1$)
 write "found"
 else
 write "Not found"
9. Exit

C function →

```
int linear_search(int A[], int N, int e)
{
    int i, f=0;
    for (i=0; i<N; i++)
    {
        if (e == A[i])
            f=1;
    }
    return(f);
}
```

```

int main()
{
    int A[30], i, N, e, f;
    printf("Enter No. of elements");
    scanf("%d", &N);
    printf("Enter array elements");
    for(i=0; i<N; i++)
        scanf("%d", &A[i]);
    printf("Enter item to be searched");
    scanf("%d", &e);

    f = linear-search(A, N, e);
    if(f==1)
        printf("found");
    else
        printf("Not found");
}

```

Binary Search → for Binary search array must be sorted.

conct →

↓ l		M=5			h ↓
10	20	30	40	50	
0	1	2	3	4	

e = 40

set l = 0 and h = N - 1 = 4

while (l ≤ h) repeat

mid = (l + h) / 2

if (e == A[mid])

return found

else if (e > A[mid])

l = mid + 1

else

r = mid - 1

if (l > h)
not found

$$l=0 \quad h=4$$

$$l \leq h \Rightarrow 0 \leq 4 \Rightarrow T$$

$$mid = (l+h)/2 = (0+4)/2 = 2$$

$$e == A[mid] \Rightarrow 40 == A[2] = 30 \Rightarrow F$$

$$e > A[mid] \Rightarrow 4 > 30 \Rightarrow T$$

$$l = mid + 1 = 2 + 1 = 3$$

again $l \leq h \Rightarrow 3 \leq 4 \Rightarrow T$

$$mid = (l+h)/2 = (3+4)/2 = 7/2 = 3$$

$$e == A[mid] \Rightarrow 40 == 40 \Rightarrow T$$

found

case 2 $\rightarrow$

$$e = 60$$

$$l=0 \quad h=4$$

$$l \leq h \Rightarrow 0 \leq 4 \Rightarrow T$$

$$mid = (0+4)/2 = 2$$

$$60 == 30 \Rightarrow F$$

$$60 > 30 \Rightarrow T$$

$$l = mid + 1 = 2 + 1 = 3$$

Again $l \leq h \Rightarrow 3 \leq 4$

$$mid = (3+4)/2 = 3$$

$$60 == 40 \Rightarrow F$$

$$60 > 40 \Rightarrow T$$

$$l = mid + 1 = 4$$

Again.

$$l \leq h \Rightarrow 4 \leq 4 \Rightarrow T$$

$$mid = (4+4)/2 = 4$$

$$e == A[mid] = 60 == 50 \Rightarrow F$$

$$60 > 50 \Rightarrow T$$

$$l = mid + 1 = 4 + 1 = 5$$

Again $l \leq h \Rightarrow 5 \leq 4 \Rightarrow F$

$$l > h \Rightarrow 5 > 4 \Rightarrow T$$

not found

Algorithm →

Binary-search ($A[\text{maxsize}]$, item)

1. Set $l = \text{LB}$ and $h = \text{UB}$
2. Repeat step 3 & 4 while ($l \leq h$)
3. Set $\text{mid} = (l + h) / 2$
4. if ($e == A[\text{mid}]$)
 write "found"
 else if ($e > A[\text{mid}]$)
 $l = \text{mid} + 1$
 else
 $h = \text{mid} - 1$
 [END of if]
 [END of while loop]
5. if ($l > h$)
 write "Not found"
6. Exit.

C function →

```
int binary-search(int A[], int N, int e)
{
    int l = 0, h = N - 1, mid, f = 0;
    while (l < h)
    {
        mid = (l + h) / 2;
        if (e == A[mid])
        {
            f = 1; break;
        }
        else if (e > A[mid])
            l = mid + 1;
        else
            h = mid - 1;
    }
}
```

```

    }
    return(f);
}

int main()
{
    int A[30], i, N, e, f;
    printf printf("Enter Array size");
    scanf("%d", &N);
    printf("Enter array elements");
    for(i=0; i<N; i++)
        scanf("%d", &A[i]);
    printf("Enter item to be searched");
    scanf("%d", &e);
    f = binary-search(A, N, e);
    if(f == 1)
        printf("found");
    else
        printf("Not found");
}

```

Binary search (Recursive method) →

```

int binary-search(int A[], int l, int h, int e)
{
    int mid;
    if(l <= h)
    {
        mid = (l+h)/2;
        if(e == A[mid])
            return 1;
    }
}

```

else if (e > A[mid])

binary-search(A, mid+1, h, e);

else

binary-search(A, l, mid-1, e);

} return -1;

int main()

{

int A[30], i, N, l, h, f, e;

printf("Enter array size");

scanf("%d", &N);

printf("Enter array elements");

for (i=0; i<N; i++)

scanf("%d", &A[i]);

printf("Enter element to be searched");

scanf("%d", &e);

l=0;

h=N-1;

f= binary-search(A, l, h, e);

if (f == 1)

printf("Found");

else

printf("Not found");

Indexed sequential search

0	1	2	3	4	5	6	7	8
11	22	33	44	55	66	77	88	99

item $\rightarrow$ 88

Set Group size = 3

$$i = 0 \quad \text{if } (\text{item} > A[i]) = 88 > 11 \Rightarrow F$$

$$i = i + gs = i + 3 = 0 + 3 = 3 \Rightarrow i = 3 \quad 88 > 44 \Rightarrow F$$

$$i = 3 + 3 = 6 \quad 88 > 77 \Rightarrow F$$

$$i = 6 + 3 = 9 \quad i < N \Rightarrow 9 < 9 \Rightarrow F$$

$$\text{set } p = i - gs = 9 - 3 = 6$$

Apply Linear Search for $i = p$ to $i = p + gs$

found

Algorithm $\rightarrow$

Indexed-sequential-search()

1. read searched item
2. Divide the array into groups according to group size. (gs)
3. Set $i = LB$
4. Repeat step while ($i \leq UB$)
5. if (item $>$ $A[i]$)
break
6. $i = i + gs$
7. set $p = i - gs$

for $i = p$ to q

8. set $i = p$
9. repeat step 10 till while ($i \leq p + q$)
10. if (item = $A[i]$)
write printf("Found");
break; [END of if]
11. $i = i + 1$; [END of loop]
12. if ($i == p + q$) then
write "Not found"
13. exit.

Sorting → To arrange the elements in a particular sequence either in ascending order or descending order.

1) Bubble sort → (process)
Arrange in ascending order

$N = 4$

40 30 20 10
 ↘ swap ↗

if $a[0] > a[1]$ then swap($a[0], a[1]$)

30 40 20 10
 ↘ swap ↗

$a[1] > a[2]$ then swap($a[1], a[2]$)

30 20 40 10
 ↘ swap ↗

$a[2] > a[3]$ then swap($a[2], a[3]$)

30 20 10 40

} pass-1

Now no more comparison left. And array is also not in ascending order. What happen? largest element is in

Indexed sequential search -

```
int index-sequential-search(int a[], int n, int item)
{
    int g, s, i, p;
    if (item < a[0] || item > a[n-1])
        return -1;
    else
    {
        printf("Enter group size");
        scanf("%d", &g);
        for (i = 0; i < n; i = i + g)
        {
            if (item < a[i])
                break;
        }
        p = i - g;
        for (i = p; i < p + g, i++)
        {
            if (item == a[i])
                return 1;
        }
        return -1;
    }
}

void main()
{
    int a[30], i, N, item, f;
    printf("Enter size");
    scanf("%d", &N);
    printf("Enter array elements");
    for (i = 0; i < N; i++)
        scanf("%d", &a[i]);

    printf("Enter search item");
    scanf("%d", &item);
    f = index-sequential-search(a, n, item);
    if (f == 1)
        printf("found");
    else
        printf("Not found");
}
```

last position. Now go to pass-2.

30 20 10 40
↖ swap ↘

again repeat the same process

$a[0] > a[1]$ then swap ($a[0], a[1]$)

20 30 10 40
↖ ↘

$a[1] > a[2]$ swap ($a[1], a[2]$)

20 10 30 40

} pass-2

next comparison is not required as 40 is already sorted. so in every next pass we have one less comparison.

now array is still not sorted. so go to pass-3

20 10 30 40
↖ ↘

$a[0] > a[1]$ so swap ($a[0], a[1]$)

10 20 30 40

} pass-3

now array is sorted so stop here.

concept → for $N=4$

- Two things are repeated. so two loops are required one for pass say (i) and another for comparison (j).
- In every pass, we perform all comparisons. so i is outer loop and j is inner loop (nesting)
- for $N=4$ total pass is 3. so outer loop is
 $\text{for } (i=1, i < N; i++)$

- $N=4$

pass 1 $i=1$ comp = 3

pass 2 $i=2$ comp = 2

pass 3 $i=3$ comp = 1

so for i th pass there are
($N-i$) comparison.

inner loop is

for ($j=1; j \leq N-i; j++$)

- In inner loop, we compare previous element say $a[j]$ to next element $a[j+1]$.

if ($a[j] > a[j+1]$)

swap($a[j], a[j+1]$)

- But if start j from 1. then for every pass first comparison is $a[1] > a[2]$. But first comparison is $a[0] > a[1]$. so j starts from 0. But total comparison is $n-i$.

so inner loop is for ($j=0; j \leq N-i-1; j++$)

Algorithm $\rightarrow$

void Bubble-sort($A[\text{maxsize}], N$)

~~1. read array size (N)~~

~~2. read array elements~~

1. for ($i=1$ to $N-1$)

for ($j=0$ to $N-i-1$)

if ($a[j] > a[j+1]$) then

swap($a[j], a[j+1]$)

[End of inner loop]

2. write array [End of outer loop]

3. Exit.

C program →

```
void bubble_sort(int A[], int N)
```

```
{
```

```
    int i, j, t;
```

```
    for (i = 1; i < N; i++)
```

```
    {
```

```
        for (j = 0; j < N - i; j++)
```

```
        {
```

```
            if (a[j] > a[j+1])
```

```
            {
```

```
                t = a[j];
```

```
                a[j] = a[j+1];
```

```
                a[j+1] = t;
```

```
            }
```

```
        }
```

```
    }
```

```
}
```

```
int main()
```

```
{
```

```
    int a[30], i, N;
```

```
    printf("Enter array size");
```

```
    scanf("%d", &N);
```

```
    printf("Enter array elements");
```

```
scanf("%d", &a[i]);
```

```
    for (i = 0; i < N; i++)
```

```
        scanf("%d", &a[i]);
```

```
    printf("Before sorting array is");
```

```
    for (i = 0; i < N; i++)
```

```
        printf("%d", a[i]);
```

```

bubble-sort(a, N);
printf("After sorting array is");
for(i=0; i<N; i++)
    printf("%d", a[i]);
}

```

2) Selection sort → process-1

$N = 5$

0	1	2	3	4	5
10	12	8	22	16	
↑	↑			↑	
min	j			j	

for(i=0; i<N-1; i++)
 min = a[i]
 for(j=i+1; j<N; j++)

$i = 0$ $\text{min} = a[i] = a[0] = 10$

$j = i+1$ $j = 1$ if ($a[j] < \text{min}$) $\Rightarrow a[1] < \text{min}$
 $\Rightarrow 12 < 10$ False update $j = 2$

$j = 2$ if ($a[2] < \text{min}$) $\Rightarrow 8 < 10 \Rightarrow T$
 $\text{min} = a[2] = 8$

$j = 3$ if ($a[3] < \text{min}$) $\Rightarrow 22 < 8 \Rightarrow F$
 update $j = 4$

$j = 4$ if ($a[4] < \text{min}$) $\Rightarrow 16 < 8 \Rightarrow F$
 update $j = 5$

$j = 5$ outside the array
 swap ($a[i]$ & min) $\Rightarrow$ swap ($a[0]$, min)
 $\Rightarrow$ swap (10, 8)

$i = 0$
pass-1

now the array is

8 12 10 22 16

pass 1 complete when j is outside the array. But array is not sorted. Then go to pass-2.

$\begin{array}{ccccc} 8 & 12 & 10 & 22 & 16 \\ 0 & 1 & 2 & 3 & 4 \\ \downarrow i & \uparrow j & & & \\ & \text{min} & \text{min} & & \end{array}$
 $i=1$ $\text{min} = a[1] = 12$

$j=2$ $a[j] < \text{min} \Rightarrow a[2] < \text{min} \Rightarrow 10 < 12 = \text{True}$
 $\text{min} = 10$

$j=3$ $a[3] < \text{min} \Rightarrow 22 < 10 \Rightarrow \text{F}$

$j=4$ $a[4] < \text{min} \Rightarrow 16 < 10 \Rightarrow \text{F}$

$j=5$ inner loop terminates

$\text{swap}(a[i], \text{min}) = \text{swap}(12, 10)$. Array is still not sorted.
 goto pass-3.

$\begin{array}{ccccc} 8 & 10 & 12 & 22 & 16 \\ 0 & 1 & 2 & 3 & 4 \\ & & \uparrow i & \downarrow j & \\ & & \text{min} & & \end{array}$
 $i=2$ $\text{min} = a[2] = 12$

$j=3$ $a[3] < \text{min} \Rightarrow 22 < 12 \Rightarrow \text{F}$

$j=4$ $a[4] < \text{min} \Rightarrow 16 < 12 = \text{F}$

$j=5$ outside the inner loop.

$\text{swap}(a[i], \text{min}) \Rightarrow$ both are same so no swapping

still not sorted goto pass 4.

$\begin{array}{ccccc} 8 & 10 & 12 & 22 & 16 \\ 0 & 1 & 2 & 3 & 4 \\ & & & \downarrow i & \downarrow j \\ & & & \text{min} & \end{array}$

$i=3$ $\text{min} = a[3] = 22$

$j=4$ $a[4] < \text{min} \Rightarrow 16 < 22 \Rightarrow \text{T}$

$\text{min} = a[4] = 16$

$j=5$ inner loop terminates. $\text{swap}(a[i], \text{min}) \Rightarrow \text{swap}(16, 22)$

8 10 12 16 22

now array is sorted. stop.

Algorithm →

selection-sort($A[\text{maxsize}], N$)

1. for ($i = 0$ to $N-2$)

 Set $\text{min} = i$

 for ($j = i+1$ to $N-1$)

 if ($A[j] < A[\text{min}]$)

$\text{min} = j$

 [End of inner loop]

 swap($A[i], A[\text{min}]$),

 [End of outer loop]

2. Exit

C program →

void selection-sort(int $A[]$, int N)

{

 int i, j, min, t ;

 for ($i = 0; i < N-1; i++$)

 {

$\text{min} = i$;

 for ($j = i+1; j < N; j++$)

 {

 if ($A[j] < A[\text{min}]$)

$\text{min} = j$;

 }

$t = A[i]$;

$A[i] = A[\text{min}]$;

$A[\text{min}] = t$;

```

}
}
int main()
{
    int A[30], i, N;
    printf("Enter array size");
    scanf("%d", &N);
    printf("Enter array elements");
    for (i=0; i<N; i++)
        scanf("%d", &A[i]);
    printf("Before sorting Array is");
    for (i=0; i<N; i++)
        printf("%d", A[i]);
    selection_sort(A, N);
    printf("After sorting. Array is");
    for (i=0; i<N; i++)
        printf("%d", A[i]);
}

```

Insertion sort →

concept →

$N=5$
 $A[]$ 12 11 13 5 6
 ↑ ↑
 j key

Pass 1 →

for $i=1$ set $key = A[i] = 11$
 $j = i-1 = 0$

compare key elements to all the previous element
 until $key < A[j]$ and $j \geq 0$

$11 < 12$ and $j=0$ if true. then
 move $A[j]$ to one position right and set $j=j-1$.
 ($A[j+1] = A[j]$)
 otherwise set $A[j+1] = key$.

$A[2] = A[1]$ and $A[0] = \text{key}$.

0	1	2	3	4
11	12	13	5	6
	$\uparrow_j$	$\uparrow_{\text{key}}$		

Pass-2

$i = 2$

~~$\text{key} = A[i] = A[2] = 13$~~

$j = i - 1 = 2 - 1 = 1$

now $\text{key} > A[j]$ i.e. $13 > 12$ and $j \geq 0$ so
move $A[j]$ to right i.e. $A[2] = A[1]$ and $j = 1 - 1 = 0$.

11	12	12	5	6
$\uparrow_j$				

~~now again~~

Pass-2

$i = 2$

$\text{key} = A[2] = 13$

$j = 1$

11	12	13	5	6
	$\uparrow_j$	$\uparrow_{\text{key}}$		

$\text{key} < A[j] \Rightarrow 13 < 12 \Rightarrow \text{False}$ so

$A[j+1] = \text{key} \Rightarrow A[3] = \text{key}$ which is already in place.

Pass-3

$i = 3$

0	1	2	3	4
11	12	13	5	6
		$\uparrow_j$	$\uparrow_{\text{key}}$	

$\text{key} = A[3] = 5$ $j = 2$

$(\text{key} < A[j] \text{ AND } j \geq 0) \Rightarrow 5 < 13$ and $j = 2 \geq 0 \Rightarrow \text{True}$

so move $A[2]$ to $A[3]$ $A[3] = A[2] = 13$ and $j = 1$

11	12	13	13	6
	$\uparrow_j$			

Again $\text{Key} < A[i]$ and $j \geq 0 \Rightarrow 5 < 12$ and $1 \geq 0 \Rightarrow T$

move $A[i]$ to $A[j]$ which gives,
and $j = 0$

11 12 12 13 6
↑
j

Again. $\text{Key} < A[j]$ and $j \geq 0 \Rightarrow 5 < 11$ and $0 \geq 0 \Rightarrow T$

move $A[j]$ to $A[i]$ and $j = -1$

↑
j 11 11 12 13 6

now $j \geq 0$ is false so go outside the loop. and

set $A[j+1] = \text{Key} \Rightarrow A[0] = 5$ which gives

0 1 2 3 4
5 11 12 13 6
↑ ↑ ↑ ↑ ↑
j key

Pass 4- $i = 4$

$\text{Key} = A[i] = 6$ $j = i - 1 = 4 - 1 = 3$

check $\text{Key} < A[j]$ and $j \geq 0 \Rightarrow 6 < 13$ and $3 \geq 0 \Rightarrow T$

move $A[j]$ to $A[i]$ and $j = 3 - 1 = 2$

0 1 2 3 4
5 11 12 13 13
↑ ↑ ↑ ↑ ↑
j key

Again check ($\text{Key} < A[j]$ and $j \geq 0$) $\Rightarrow 6 < 12$ and $2 \geq 0 \Rightarrow T$

move $A[j]$ to $A[i]$ and $j = 2 - 1 = 1$

5 11 12 12 13
↑ ↑ ↑ ↑ ↑
j key

Again check ($\text{key} < A[j]$ and $j >= 0$)

$6 < 11$ and $j >= 0 \Rightarrow T$

move $A[1]$ to $A[2]$ and $j = 1 - 1 = 0$

0	1	2	3	4
5	11	11	12	13

$\uparrow$
 j
Again check ($\text{key} < A[j]$ and $j >= 0$) $\Rightarrow 6 < 5$ and $0 >= 0 \Rightarrow F$
Set $A[j+1] = \text{key} \Rightarrow A[1] = \text{key} = 6$ which gives

5 6 11 12 13

Now array is sorted.

Algorithm $\rightarrow$

~~insertion~~ $\text{insertion-sort}(A[\text{maxsize}], N)$

1. for ($i = 1$ to $N-1$)
2. Set $\text{key} = A[i]$
3. Set $j = i - 1$
4. while ($j >= 0$ AND $A[j] < \text{key}$)
5. Set $A[j+1] = A[j]$
6. $j = j - 1$
- [End of while loop]
7. Set $A[j+1] = \text{key}$
- [End of for loop]
8. Exit.

C ~~pro~~ function →

```
void insertion-sort(int A[], int N)
{
```

```
    int key, i, j;
```

```
    for (i = 1; i < N; i++)
    {
```

```
        key = A[i];
```

```
        j = i - 1;
```

```
        while (j >= 0 && key < A[j])
        {
```

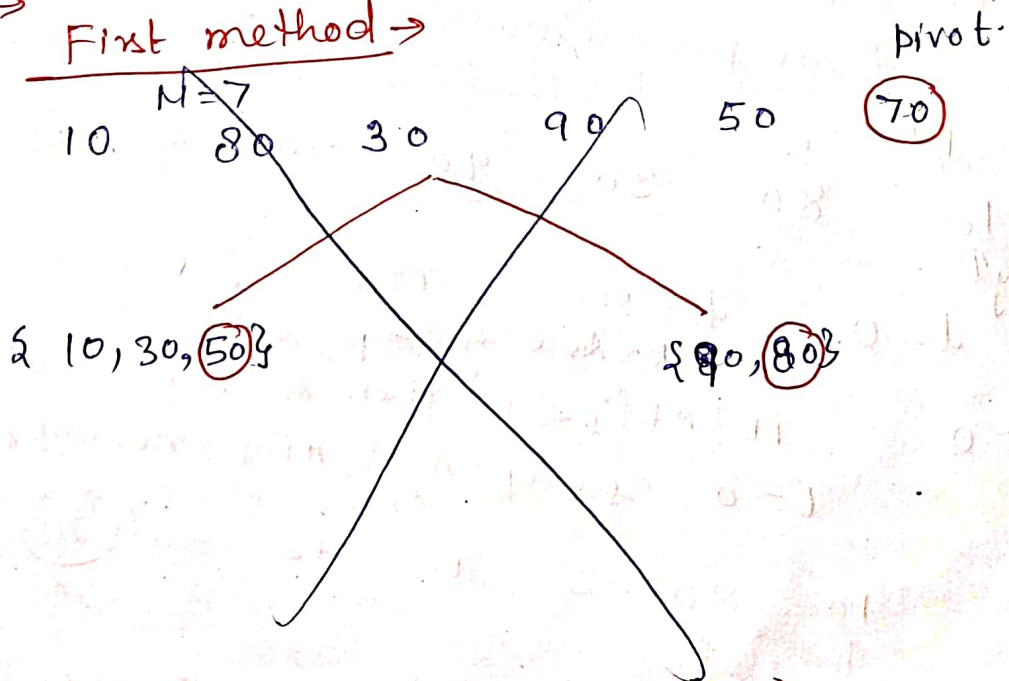
```
            A[j+1] = A[j];
```

```
            j = j - 1;
```

```
        }
```

```
        A[j+1] = key;
```

```
    }
```

Quick sort →First method →concept →

Quick sort

$M=7$

{ 10, 80, 30, 90, 40, 50, 70 }

{ 10, 30, 40, 50 }

{ 80, 90 }

{ 10, 30, 40 }

{ }

{ 80 }

{ }

{ 10, 80 }

{ }

{ 10 }

In Quick sort we take last elements as a pivot element. and partition Array into two subarray such that left subarray contains elements less than the pivot element and right subarray contains elements greater than pivot element.

process for partitioning.

$i \downarrow$
 -1
 $0 \downarrow l$
 10
 $j \uparrow$
 $l=0$
 1
 80
 2
 30
 3
 90
 4
 40
 5
 50
 6
 70
 h
 p
 $h = M-1 = 7-1 = 6$
 $l = l-1 = 0-1 = -1$
 $p = A[h] = 70$

$j=0$
 if $(A[j] < P)$ then set $i=i+1$ and swap $(A[i], A[j])$ and $j=j+1$
 $i=0$ swap $(A[i], A[j]) \Rightarrow$ no change. $j=1$

$j=1$

10
 80
 30
 90
 40
 50
 70
 i
 j
 p

$\neg (A[j] < P) \Rightarrow A[j] \geq P \Rightarrow 80 \geq 70 \Rightarrow F$ then set $j=j+1$

$j \geq 2$

10 80 30 90 40 50 (70)
↑ ↑ ↑ ↑
i i j p

$A[j] < P \Rightarrow A[2] < P \Rightarrow 30 < 70 \Rightarrow T$

$i = i + 1 = 1$

$\text{swap}(A[i], A[j]) \Rightarrow \text{swap}(A[1], A[2])$
 $j = j + 1$

10 30 80 90 40 50 (70)
↑ ↑ ↑ ↑
i i j p

$j = 3$ $A[j] < P \Rightarrow A[3] < P \Rightarrow \text{False}$ set $j = j + 1$

$j = 4$ 10 30 80 90 40 50 (70)
↑ ↑ ↑ ↑ ↑
i i i j p

$A[j] < P \Rightarrow 40 < 70 \Rightarrow T$

$i = i + 1 = 2$

$\text{swap}(A[i], A[j]) \Rightarrow \text{swap}(A[2], A[4])$

$j = j + 1 = 5$

$j \geq 5$ 0 1 2 3 4 5 6
10 30 40 90 80 50 (70)
↑ ↑ ↑ ↑ ↑ ↑
i i i i i j p

$A[j] \leq P \Rightarrow A[5] < P \Rightarrow 50 < 70 \Rightarrow T$

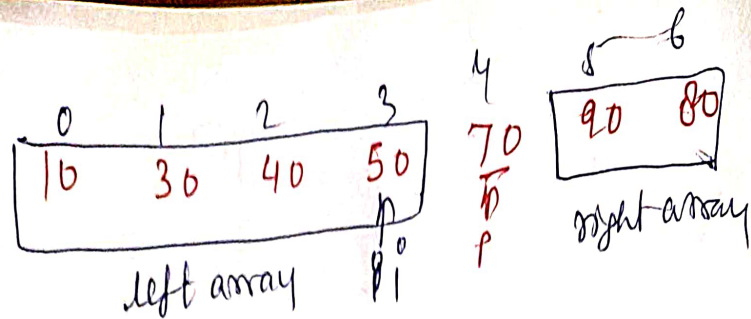
$i = i + 1 = 3$

$\text{swap}(A[3], A[5])$ and $j = 5 + 1 = 6$

10 30 40 50 80 90 (70)
↑ ↑ ↑ ↑
i i j p

$j > \text{high} - 1 \Rightarrow \text{False}$ $j > 5 \Rightarrow 6 > 5 \Rightarrow F$

now $\text{swap}(A[i+1], P)$



$\text{return}(i+1) \Rightarrow \underline{\underline{\text{return}(4)}}$

now Apply partitioning process for left and right subarray recursively.

Algorithm

$\text{partition}(A[], l, h)$

1. $p = A[h]$

2. $i = l - 1$

3. for $(j = l \text{ to } h - 1)$

if $(A[j] < p)$ then

set $i = i + 1$

swap $(A[i], A[j])$

[End of if]

[End of for loop]

4. swap $(A[i+1], A[h])$

5. return $(i+1)$

$\text{Quicksort}(A[], l, h)$

if $(l < h)$

$p = \text{partition}(A, l, h)$

$\text{Quicksort}(A, l, p-1)$

$\text{Quicksort}(A, p+1, h)$

[End of if]

C program →

```
void swap(int *a, int *b)
{
    int t = *a;
    *a = *b;
    *b = t;
}
```

```
int partition(int A[], int l, int h)
{
    int p, i = -1, j;
    p = A[h];
    for (j = 0; j < h; j++)
    {
        if (A[j] < p)
        {
            i++;
            swap(&A[i], &A[j]);
        }
    }
    swap(&A[i+1], &A[h]);
    return (i+1);
}
```

```
void quicksort(int A[], int l, int h)
{
    int p;
    if (l < h)
    {
        int p = partition(A, l, h);
        quicksort(A, l, p-1);
        quicksort(A, p+1, h);
    }
}
```

```
int main()
```

```
{
```

```
    int A[30], d, n;
```

```
    printf("Enter size");
```

```
    scanf("%d", &n);
```

```
    printf("Enter array elements");
```

```
    for (i=0; i<n; i++)
```

```
        scanf("%d", &A[i]);
```

```
        quicksort(A, 0, n-1);
```

```
    printf("After sorting");
```

```
    for (i=0; i<n; i++)
```

```
        printf("%d", A[i]);
```

```
}
```

Second method →

N = 6

↓ left
12
↑
P

15

13

7

6

right
14
↑
h

left = l

right = h

p = l

while(1)

check $A[r] > A[p]$ and $right \neq p$

right = right - 1

if (right == p)

break

swap($A[right]$, $A[p]$)

p = right

10

6
↑
left

15

13

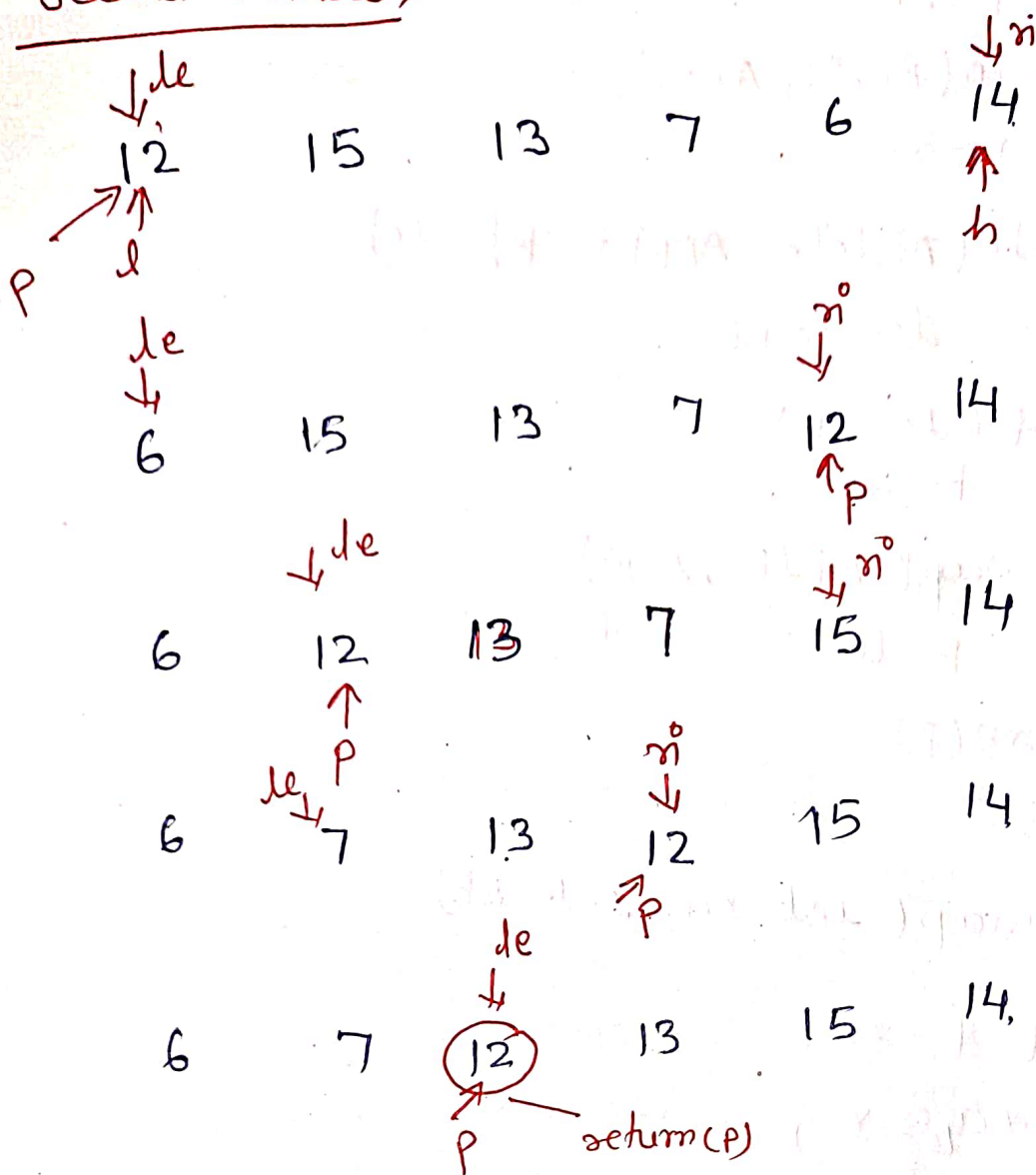
7

12

14

↑↑ right
P

Second method →



Algorithm

$\text{quick_sort}(A, l, h)$

if $(l < h)$ then

$p = \text{partition}(A, l, h)$

$\text{quick_sort}(A, l, p-1)$

$\text{quick_sort}(A, p+1, h)$

$\text{partition}()$

$le = l, ri = h, p = l$

while(1)

while $(A[ri] \geq A[p] \ \&\& \ p \neq ri)$

$ri = ri - 1$

```

    if (i == p)
        break
    swap(A[i], A[p])
    p = i
    while (A[l] <= A[p] && p != l)
        l = l + 1
    if (l == p)
        break
    swap(A[l], A[p])
    p = l
    return(p)

```

C program →

```

void swap(int *a, int *b)
{
    int t = *a;
    *a = *b;
    *b = t;
}

int partition(int A[], int l, int h)
{
    int le = l, ri = h, p = l;
    while(1)
    {
        while (A[ri] >= A[p] && p != ri)
            ri = ri - 1;
        if (p == ri)
            break;
        swap(&A[p], &A[ri]);
        p = ri;
    }
}

```

```
while ( A[le] <= A[p] && p != le )
```

```
    le = le + 1;
```

```
if ( p == le )
```

```
    break;
```

```
    swap( &A[p], &A[le] );
```

```
    p = le;
```

```
}
```

```
return( p );
```

```
}
```

```
void modified quicksort( int A[], int l, int h )
```

```
{
```

```
    int p;
```

```
    if ( l < h )
```

```
    {
```

```
        p = partition( A, l, h );
```

```
        quicksort( A, l, p-1 );
```

```
        quicksort( A, p+1, h );
```

```
    }
```

```
}
```

```
void main( )
```

```
{
```

```
    int A[30], i, N;
```

```
    printf( "Enter array size" );
```

```
    scanf( "%d", &N );
```

```
    printf( "Enter array elements" );
```

```
    for for ( i=0; i<N; i++ )
```

```
        scanf( "%d", &A[i] );
```

```
    quicksort( A, 0, N-1 );
```

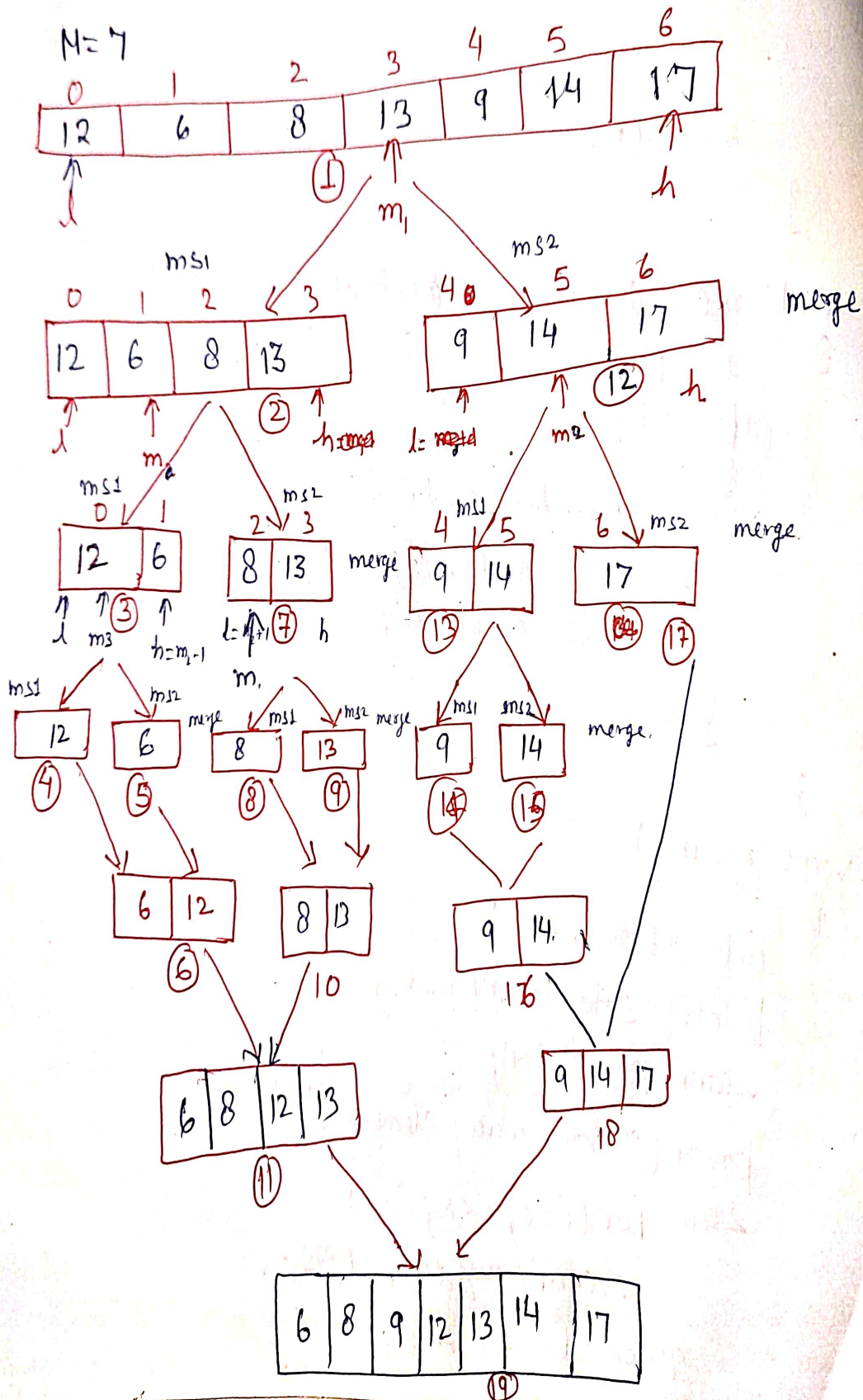
```
printf("sorted array is");
```

```
for(i=0; i<N; i++)
```

```
printf("%d", A[i]);
```

```
}
```

mergesort →



Algorithm →

mergesort($A[l, h]$, l , h)

1. ~~mergesort~~ if ($l < h$)
2. $m = (l + h) / 2$
3. call mergesort(A, l, m)
4. call mergesort($A, m+1, h$)
5. merge(A, l, m, h)
6. Exit.

merge(A, l, m, h)

1. set $i = l$
 $j = m+1$
 $k = l$
2. repeat ~~stop~~ while ($i \leq m$ and $j \leq h$)
 if ($A[i] < A[j]$)
 temp[k] = $A[i]$
 $k = k+1$
 $i = i+1$
 else
 temp[k] = $A[j]$
 $k = k+1$
 $j = j+1$
 [End of if]
 [End of while]

while ($i \leq m$)

temp[k] = A[i]

k = k + 1

i = i + 1 [end of while]

while ($j \leq h$)

temp[k] = A[j]

k = k + 1

j = j + 1 [End of while]

for (c = 0 to k - 1)

A[i] = temp[i]

exit.

C program →

void merge(int a[], int l, int m, int h)

{

int temp[30], i, j, k;

i = l

j = m + 1

k = l

while ($i \leq m$ & $j \leq h$)

{

if (a[i] < a[j])

temp[k++] = a[i++];

else

temp[k++] = a[j++];

}

while ($i \leq m$)

temp[k++] = a[i++];

```

while (j <= h)
    temp[k++] = a[j++];
for (i = 0; i < k; i++)
    a[i] = temp[i];
}

```

```

void mergesort(int a[], int l, int h)
{
    int m;
    if (l < h)
    {
        m = (l + h) / 2;
        mergesort(a, l, m);
        mergesort(a, m + 1, h);
        merge(a, l, m, h);
    }
}

```

```

int main()
{
    int a[30], i, n;
    printf("Enter size of array");
    scanf("%d", &n);
    printf("Enter array elements");
    for (i = 0; i < n; i++)
        scanf("%d", &a[i]);
    mergesort(a, 0, n - 1);
    printf("After sorting array elements are");
    for (i = 0; i < n; i++)
        printf("%d", a[i]);
}

```

Radix sort $\Rightarrow$ To sort decimal number where radix or base is 10, we need 10 packets. These packets are numbered 0, 1, 2, 3, ..., 9. numbers are stored from right digit to left digit.

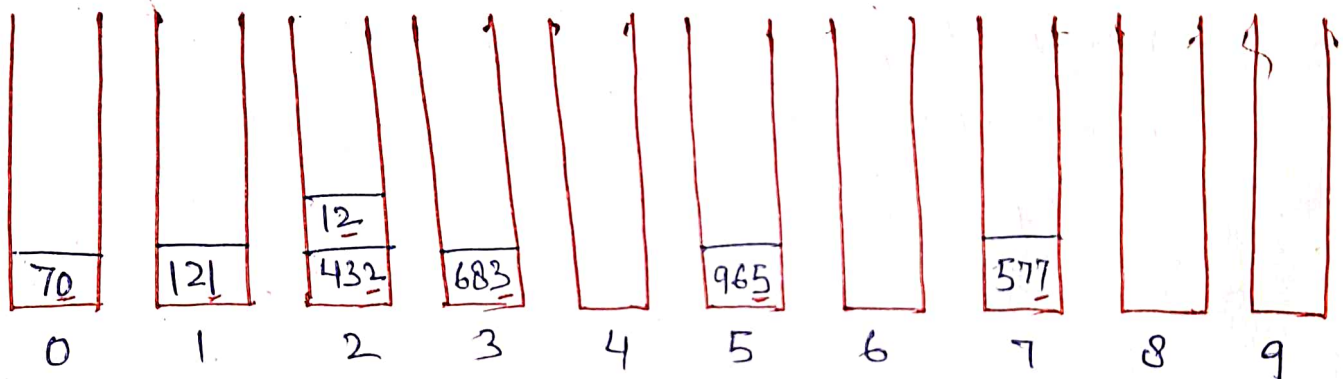
number of required passes = no. of digits in largest number.

* for storing names we need 26 packets.

Example - sort 121, 70, 965, 432, 12, 577, 683

largest no = 965

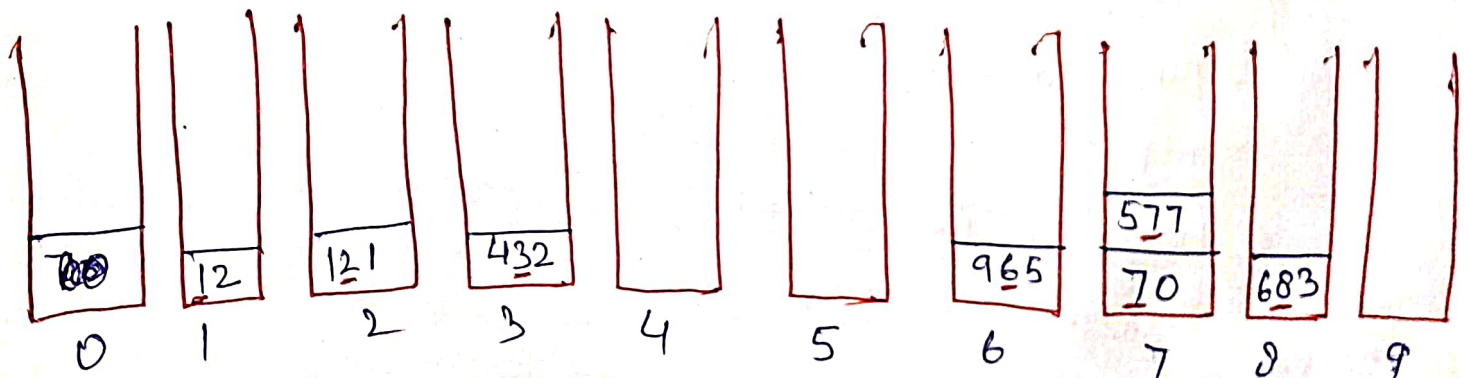
no. of passes required = 3. The numbers are stored in packets according to unit digit.



After 1st pass result array is

70, 121, 432, 12, 683, 965, 577

Now the numbers are stored according to Ten's digit.



After second pass resulted array is

012, 121, 432, 965, 070, 577, 683

Now the numbers are stored according to hundred's digit.

070 12	121			432	577	683			965
0	1	2	3	4	5	6	7	8	9

After Third or last pass resulted array is
12, 70, 121, 432, 577, 683, 965

C program Algorithm

1. Find the largest element of the array.
2. Find the total number of digits in largest number. (n)
3. repeat steps 4 to 8 for pass ≥ 1 to n
4. repeat step 4.1 for $k \geq 0$ to 9
 - 4.1 $buck[k] = 0;$
5. repeat step 5.1 for $i \geq 0$ to $n-1$
 - 5.1 $d = (a[i] / div) \% 10$
 $pocket[d][buck[d]] = a[i]$
 $buck[d] = buck[d] + 1$
6. $i = 0$
7. repeat step 7.1 for $k \geq 0$ to 9
 - 7.1 $j = 0$ and repeat 7.2 while $j < buck[k]$
 - 7.2 $a[i] = pocket[k][j]$
 $i = i + 1$
 $j = j + 1$
8. $div = div * 10$
9. Exit.

C program →

```
void radix-sort (int a[], int n)
```

```
{
```

```
    int t, i, j, max, temp[10][30], r[10], f[10];
```

```
    int k=0, count=0, d=1, 5;
```

```
    // find max element
```

```
    max = a[0];
```

```
    for (i=1; i<n; i++)
```

```
        if (a[i] > max)
```

```
            max = a[i];
```

```
    // find no. of digits in max element
```

```
    while (max != 0)
```

```
    {
```

```
        count = count + 1;
```

```
        max = max / 10;
```

```
    }
```

```
    // logic for passes.
```

```
    for (i=1; i<=count; i++)
```

```
    {
```

```
        for (s=0; s<10; s++)
```

```
            r[s] = f[s] = -1;
```

```
        for (j=0; j<n; j++)
```

```
        {
```

```
            t = (a[j]/d) % 10;
```

```
            if (r[t] == -1)
```

```
                f[t] = r[t] = 0;
```

```
            else
```

```
                r[t] = r[t] + 1;
```

```
            temp[t][r[t]] = a[j];
```

```
        }
```

```

        d = d * 10;
    } // end of i loop

    for (i = 0; i < 10; i++)
    {
        for (j = f[i]; j <= r[i]; j++)
            if (f[i] != -1)
                a[k++] = temp[i][j];
    }

```

```

void main()
{

```

```

    int a[30], i, n;

```

```

    printf("Enter size");

```

```

    scanf("%d", &n);

```

```

    printf("Enter array elements");

```

```

    for (i = 0; i < n; i++)

```

```

        printf("%d", a[i])

```

```

    radix_sort(a, n);

```

```

    printf("After sorting array is");

```

```

    for (i = 0; i < n; i++)

```

```

        printf("%d", a[i]);

```

```

}

```

Hashing - ~~Algorithm function~~ Hashing is the process of generating a value from a text or a list of numbers using a mathematical function known as hash function.

Suppose there are n elements which are to be stored in hash table of size M where $M \geq n$.

An element with key value K will be put in slot j of hash table if $j = H(K)$

where $H[K]$ is a hash function.

It is possible that $H(K_1)$ may be same as $H(K_2)$. This is called collision. and K_1 and K_2 are called synonyms.

Different Hash function -

1) Division method - This is the most simplest and easiest method to generate a hash value. The hash function divides the value K by M and uses the remainder obtained.

$$h(K) = K \bmod M$$

where K = key value

M = size of hash table.

example →

$$K = 12345 \quad M = 95$$

$$h(K) = 12345 \bmod 95 = 90$$

$$K = 1276 \quad M = 11 \quad h(K) = 1276 \bmod 11 = 0$$

Advantages:- This method is very fast since it requires only a single division operation.

Disadvantage:-

- 1) This method leads poor performance since consecutive keys map to consecutive hash value in hash table.
- 2) Extra care should be taken to choose the value of M .

2) Mid square method - It involves two steps to compute hash value.

- 1) Square the value of key (K^2)
- 2) Extract the middle r digits as the hash value.

The value of r can be decided based on the size of a Hash Table.

Example - Let the hash table has 100 memory locations. and $key = 60$. Calculate Hash value.

Soln $r = 2$

Ans:- $M = 100$ So $r = 2$.

$$K \times K = 60 \times 60 = 3600$$

$$h(60) = 60$$

Advantages:- 1) The performance of this method is good as most or all digits of the key contribute to the result.

2) The result is not dominated by the distribution of the top digit or bottom digit of the key.

Disadvantages:- 1) The size of the key is limitation, as the key is of big size then its square will double the number of digits.

2) There will be collisions.

3) Digit Folding method - This method involves two steps:

- 1) Divide the key-value K into number of parts, i.e., $K_1, K_2, K_3, \dots, K_n$ where each part has the same number of digits except for the last part that can have lesser digits than the other parts.
- 2) Add the individual parts. The hash value is obtained by ignoring the last carry if any.

example $\rightarrow$

$$K = \underline{12} \underline{34} 5$$

$$K_1 = 12 \quad K_2 = 34 \quad K_3 = 5$$

$$S = K_1 + K_2 + K_3 = 12 + 34 + 5 = 51$$

$$H(K) = 51$$

(4) Truncation method - In this method we take only part of the key as address, it can be some rightmost digit or leftmost digit. part may depend on size of Hash table.

ex $\rightarrow$ $K = 12345$ $M = 100$ then we take either left two digit or right two digits of key.

$$H(K) = 12 \text{ or } 45$$

5) Multiplication method $\Rightarrow$

1. choose a constant A such that $0 < A < 1$
2. multiply K with A
3. Extract the fractional part of KA
4. multiply the result of step 3 by the size of Hash Table (M).
5. The resulting hash value is obtained by taking the floor of the result obtained ~~by~~ in step 4.

Example-

$$K = 123$$

$$M = 100$$

$$A = 0.35$$

1. ~~$H(K)$~~

$$1. \quad A = 0.35$$

$$2. \quad K \times A = 0.35 \times 123 = 43.05$$

$$3. \quad \text{fractional part} = 0.05$$

$$4. \quad M \times \text{fractional part} = 100 \times 0.05 = 5$$

$$5. \quad \text{floor value} = 5$$

$$H(123) = 5$$

collision conflict resolution techniques:-

There are two methods for conflict resolution

- (i) open chaining Addressing.
- (ii) Separate chaining.

1) ~~open chaining~~ open Addressing $\Rightarrow$ In open addressing, all elements an empty position is found out within the hash table itself and the new key is inserted in that empty position.

Different types:- (a) Linear probing - In linear probing, the hash table is searched sequentially that starts from the original location of the hash. If in case the location that we get is already occupied, then we check for next location.

Example $\Rightarrow$

$M = 5$

keys = 50, 70, 76, 93

1. Draw empty Hash Table

0	1	2	3	4

2. first key is 50 compute $H[K] \bmod N = 50 \% 5 = 0$. So insert into slot no. 0.

0	1	2	3	4
50				

3. next key is 70. compute $K \bmod N = 70 \% 5 = 0$. But 50 is already in slot no 0, so search for the next empty slot and insert it.

0	1	2	3	4
50	70			

4. next key is 76. $76 \% 5 = 1$ but slot no 1 is already occupied by 70. so search for next empty slot and insert it.

0	1	2	3	
50	70	76		

5. next key is 93. $93 \% 5 = 3$. slot 3 is empty. Insert 93 at slot 3.

0	1	2	3	4
50	70	76	93	

2. Quadratic probing:- In this method, we look for the i^{th} slot in the i^{th} iteration. We always starts from the original hash location. If only the location is occupied then we check the other slots.

example →

$$m = 7$$

$$K = 22, 30, 50$$

1.

0	1	2	3	4	5	6

2. $K = 22$ $22 \% 7 = 1$ slot 1 is empty, insert 22 at 1.

0	1	2	3	4	5	6
	22					

3. $K = 30$ $30 \% 7 = 2$ slot 2 is empty; insert 30 at 2.

0	1	2	3	4	5	6
	22	30				

4. $K = 50$ $50 \% 7 = 1$ slot 1 is not empty. so we will search for slot $1 + 1^2 = 2$

Again slot 2 is found occupied, so we will search for cell $1 + 2^2 = 1 + 4 = 5$. Insert 50 at 5.

0	1	2	3	4	5	6
	22	30			50	

3) Double hashing: - In this technique, the increment for the probing sequence are computed by using another hashing function. We use another hash function $hash_2(x)$ and look for the $i \times hash_2(x)$ slot in i^{th} iteration.

Example:

$$M = 7$$

$$Key = 27, 43, 92, 72$$

$$H_1(K) = K \bmod 7$$

$$H_2(K) = K \bmod 5 + 1$$

1. Create empty HashTable

0	1	2	3	4	5	6

2. Key = 27 compute $27 \% 7 = 6$. 6 is empty. insert 27 into 6.

0	1	2	3	4	5	6
						27

3. Key = 43 $43 \% 7 = 1$ slot 1 is empty. insert 43 in slot 1.

0	1	2	3	4	5	6
	43					27

4. Key = 92 $92 \% 7 = 1$. slot 1 is not empty. so apply second Hash function $1 + 92 \% 5 = 1 + 2 = 3$. slot 3 is empty. insert 92 in slot 3.

0	1	2	3	4	5	6
	43		92			27

5. Key = 72 $72 \% 7 = 2$. slot 2 is empty. insert 72 in slot 2.

0	1	2	3	4	5	6
	43	72		92		27

Separate chaining:- This method maintains the chain of elements which have same hash address.

We can take the hash table as an array of pointers

Here each pointer will point to one linked list and elements which have same hash address will be maintained in the linked list

Nodes are stored outside the space of hash table so this is called separate chaining.

example -

351, 493, 251, 71, 706, 146

$$h(k) = k \bmod 7$$

Key	351	493	251	71	706	146
$h(k)$	1	3	6	1	6	6

